# Year 1 Key **Representations** Find out more...

Watch the **Unit tutorial** before planning each unit.

Read the **planning guides** for suggestions of representations.

Make use of PD videos on unit pages and Progression in Calculations page.



**Representations of number** 

think about what this shows.

**Ordering numbers** 

**Comparing numbers** 

There are seven counters. Seven is two more than five. Seven is three less than 10.

line, within 20. These representations are used to secure counting within 20 and stating one more / one less.

There are 11 cubes, 11 is one more than ten.

1

2

3

**Representing numbers 11-20** 

4

5

Pupils say, read and write teen numbers. Pupils understand the ten

and ones relationship of teen numbers, supported by representations.

There are fourteen cubes. This is written as 14. 14 is one ten and

four ones.

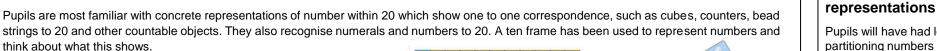
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Pupils have explored a number of ways to order and compare numbers practically using representations including a number track and a number

8

9

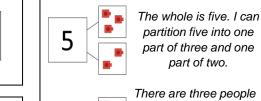
10



Pupils will have had lots of experience partitioning numbers in different ways through exploring concrete representations. They may identify these as parts and should see that numbers can be split in different ways.

Part-whole language and

A part-whole model is used to represent number bonds, addition and subtraction. Pupils are familiar with the concept of a whole and partitioning this into two or more parts. They explore how to write this relationship as an equation.



5

in one train carriage and two people in another. One part is three and one part is two. The whole is five.

whole = part + part 5 = 3 + 2

## **Development of division**

Pupils explore counting in equal groups using manipulatives or pictorial representations.

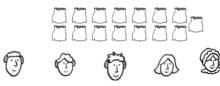


There are three equal groups of 10. 10, 20, 30. There are 30 altogether.

Pupils have explored the concept of equal and unequal grouping and sharing in context using concrete manipulatives.



15 cows can be grouped into five fields in this way. The groups are unequal.



If 15 bags of grain are shared equally between five farmers, each farmer gets three bags.

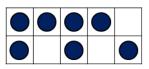
# Equations

The phrase 'is equal to' is used consistently to refer to the = symbol. What is on one side of the symbol is equal to what is on the other side. Present equations in different ways to support this: 2 + 3 = 5

5 = 3 + 2

## Counting principles – conservation of number

A key number principle for developing addition and subtraction strategies is to understand that the same number of objects will always have the same value.



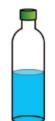
There are still seven counters. The position has changed but no counters have been added or taken away.

# **Developing fraction language**

The foundations for fractions have been laid through exploration of half full / half empty and associated descriptions. Pupils have also explored doubling and halving without linking specifically to fractions.

The bottle is half full.

The bottle is half empty.



to-one correspondence. Five is less than seven. Five ones is fewer than

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20

Concrete representations are used to compare numbers, focusing on

comparison: lining towers of cubes next to one another builds on one-

correct language use. The structure of the representation supports

seven ones. Seven is greater than five.

# Counting principles – subitising

Subitising is the ability to identify a group of objects without the need to count. Pupils have explored this and should be confident in subitising up to five objects. Making use of patterns e.g. die faces, triangle shapes can support this.



**Doubling and halving** 



Double three is six. Three plus three is equal to six. Half of six is three.

Pupils are familiar with addition and subtraction (taking away) using concrete and pictorial representations. A range of contexts for this have been explored. Pupils should be familiar with strategies including count all, count on and count back using representations.

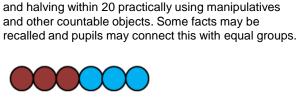
Addition and subtraction strategies

I have three red cubes and four purple cubes. I can put them together and count the whole. There are seven cubes.

count on from four: five, six. There are six cubes.

I have five cubes. I can take away two: four, three. Five take away two is three.

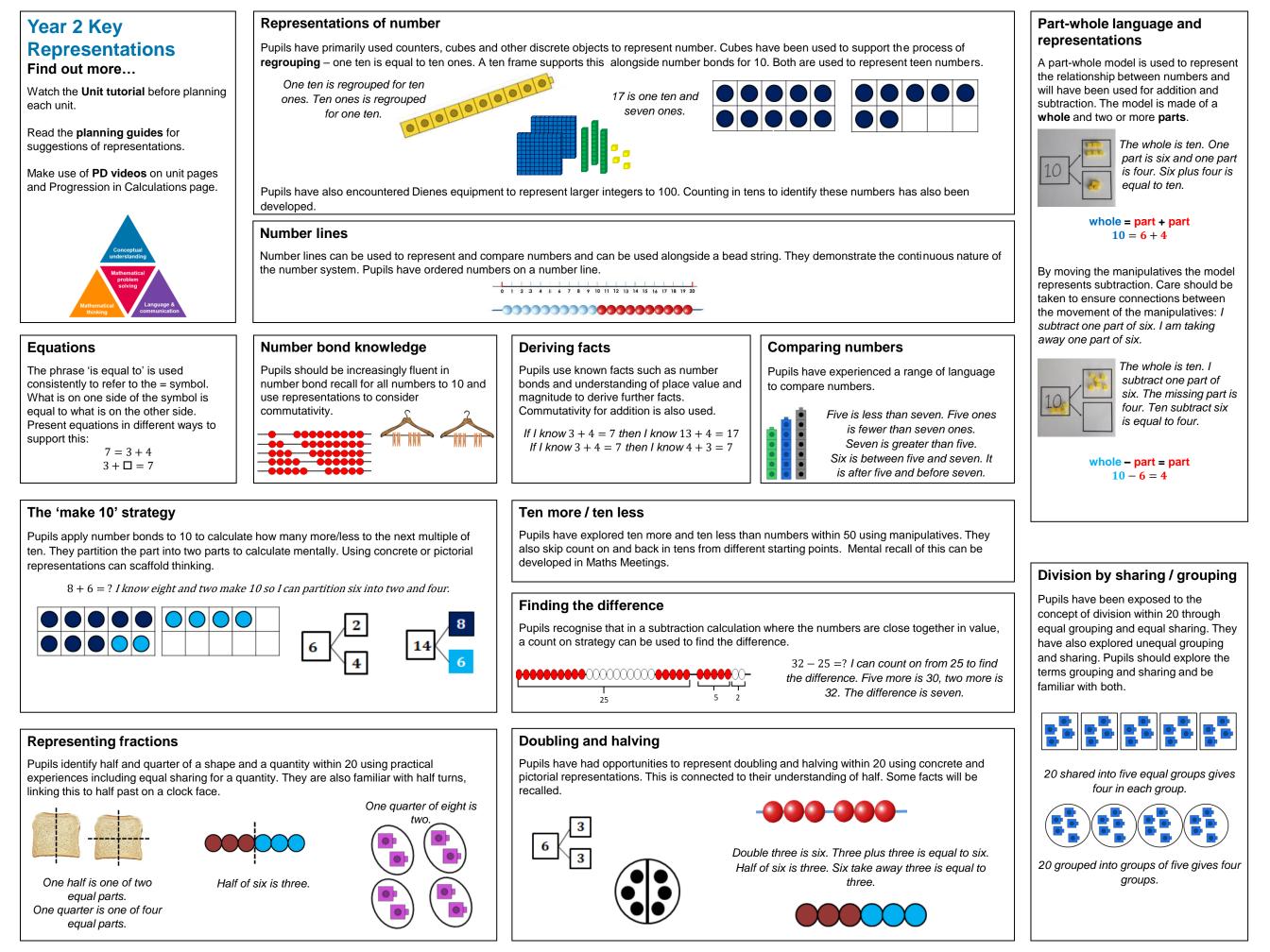




Pupils have had opportunities to represent doubling



I have four yellow cubes. I add two green cubes. I can



# Year 3 Key **Representations** Find out more...

Watch the **Unit tutorial** before planning each unit and read the Unit Narrative.

Read the **planning guides** for suggestions of representations.

Make use of PD videos on unit pages and Progression in Calculations page.

Explore the guidance for Year 3 representations.



# **Dienes equipment**

Number lines

Year 3.

An important resource for demonstrating the relative size of place value columns. Supports the process of **regrouping** – one ten is equal to ten ones, one hundred is equal to ten tens and so on. Can also be used to represent addition and subtraction with 2- and 3-digit integers.

Number lines can be used to represent and compare numbers and can be used alongside a bead string. They demonstrate the continuous nature of

the number system. When calculating, number lines may act as a jotting of the steps of a mental calculation and may begin 'empty' i.e. not have

Pupils use known facts such as number bonds

If I know 12 + 5 = 17 then 22 + 5 = 27.

*If I know* 12 + 5 = 17 *then* 17 - 12 = 5

If I know 17 - 12 = 5 then 37 - 12 = 25

and understanding of place value and

magnitude to derive further facts.

numbered divisions. Pupils will have experienced this most through adding tens then ones as shown. The use of number lines is extended during

One ten is regrouped for ten ones. Ten ones is regrouped for one ten.

Number bond knowledge

Make use of transitions and Maths

Meetings to develop this.

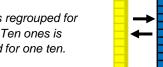
Pupils should be increasingly fluent in

number bond recall for all numbers to 20.

17 = 12 + 5

17 = 11 + 6

17 = 10 + 7







234 is two hundreds, three tens and four ones. I can represent subtracting 20 by removing two ten sticks.

+2

+20

Bead strings help support the ordinality of

the value 101-200 for representation when

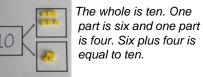
number. They are repurposed e.g. beads have

**Bead strings** 

rounding.

# Part-whole language and representations

A part-whole model is used to represent the relationship between numbers in all four operations. The model is made of a whole and two or more parts.



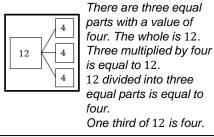
is four. Six plus four is equal to ten.

By moving the manipulatives the model represents subtraction.



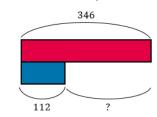
The whole is ten. I subtract one part of six. The missing part is four. Ten subtract six is equal to four.

Multiplication, division and fractions of quantities can be represented using multiple equal parts.

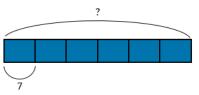


### **Bar models**

Pictorial bar models and concrete Cuisenaire as bar models are used throughout the year and represent partwhole relationships and knowns and unknowns within problems. See PD videos for further exemplification.



I know the whole is 346, and one of the parts is 112. I do not know the value of the missing part. I can subtract 112 from 346.



The value of each part is 7 and there are 6 equal parts. The whole is unknown.  $7 \times 6 = 42$ 

# Equations

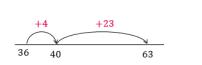
The phrase 'is equal to' is used consistently to refer to the = symbol. Equations should be presented with symbols and missing numbers in different positions:

> 38 = 25 + 13 $\Box = 37 + 44$  $12 \div \Box = 4$

# The 'make 10' strategy

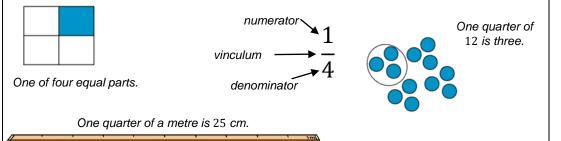
Pupils apply number bonds to 10 to calculate how many more/less to the next multiple of ten. They partition the part into two parts to calculate mentally. Using concrete or pictorial representations can scaffold thinking.

36 + 27 = ? I can partition 27 into 4 and 23. 36 plus 4 is equal to 40. 40 plus 23 is equal to 63.



# **Representing fractions**

A range of concrete and pictorial representations are used for fractions including fractions of a whole, as part of a set of objects and as part of a quantity such as a length or volume. Pupils should be familiar with a range of representations.

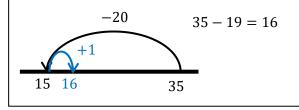


# Round and adjust

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20

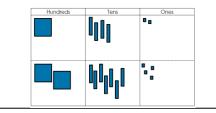
Pupils apply understanding of ordinality of number, recognising when a part or whole is close to a multiple of 10 e.g. 29, 32. They round before calculating, then adjust their answer accordingly. Concrete or pictorial models are used to represent this.

**Deriving facts** 



# **Place value charts**

Place value charts have been used to represent two-digit numbers and can be used alongside concrete, pictorial and abstract representations of number to secure understanding of the positional aspect of the number system. Pupils have made use of place value charts when adding two 2-digit numbers and their use is extended in Year 3.



# Arrays

Concrete and pictorial arrays demonstrate the commutativity of multiplication and inverse relationship of multiplication and division. Pupils should be familiar with considering rows and columns. Part-whole language may be used alongside.

> There are four parts/groups each with a value of three. The whole is 12. Four multiplied by three is equal to 12.

The whole is 12. There are three parts/groups each with a value of 4. 12 divided by three is equal to four. One third of 12 is equal to four.

# Year 4 Key **Representations** Find out more...

Watch the **Unit tutorial** before planning each unit and read the Unit Narrative.

Read the planning guides for suggestions of representations.

Make use of PD videos on unit pages and Progression in Calculations page.

### Representations of number representations Pupils are familiar with a range of concrete and pictorial representations of number with and without a place value chart. These are used to represent a number or calculation and should not be used as a counting tool. Pupils also make use of these when comparing numbers. 234 is two hundreds, three tens and four whole and two or more parts. ones. 00 312 190 90 Number lines +23Number lines can be used to represent and compare, demonstrating the continuous nature of the number system. 150 312 When calculating, number lines may act as a jotting of the steps of a mental calculation and may begin 'empty' 36 40 63 i.e. not have numbered divisions. They are also used as a representation for rounding. 72 Number fact knowledge **Deriving facts and inverse** Multiplication and division by multiplicative relationships. powers of 10 relationships Pupils know number bonds to 100 and apply to other Equations multiples of 10. Pupils are increasingly fluent in a Pupils use known facts such as number Pupils have experienced the concept of range of number facts including partitioning in 40 bonds and understanding of place value ten times greater and smaller through The phrase 'is equal to' is used different ways to discuss number. and magnitude to derive further facts. exchanging Dienes, linking this to the consistently to refer to the = symbol. 136 is multiple of 4 because I can see 120 and 16 apparent move of digits in a place value Equations should be presented with 120 40 If I know 12 + 5 = 17 then 222 + 5 = 227which are both multiples of 4. chart. to 120. symbols and missing numbers in If I know $3 \times 4 = 12$ then I know $6 \times 4 = 24$ different positions: They are also familiar with multiplication tables for 2,

Inverse relationships have also been

If I know 12 + 5 = 17 then 17 - 12 = 5

If I know  $3 \times 4 = 12$  then I know  $12 \div 4 = 3$ 

explored.

597

600

38 = 25 + 13 $\Box = 37 + 44$  $12 \div \Box = 4$ 

 $6 \times 8 = 48$   $48 \div 8 = 6$ 

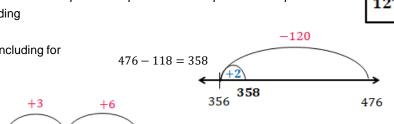
3, 4, 5, 6, 8 and 10 and related division facts.

Make use of transitions and Maths Meetings to develop this.

# **Mental strategies**

Pupils have experienced a range of mental strategies for all four operations, including:

- Applying number bonds to 10 and 100 to calculate how many more/less to the next multiple of ten, extending to 100 and 1000, using the 'make 10' strategy.
- Identifying numbers close to a multiple of ten or 100 e.g. 28, 201 and using a round and adjust strategy, including for multiplication. "If I know 20 x 4 is 80, then 19 x 4 is 76".
- Identifying near doubles for addition. 43 and 45 can be seen as 'double 43 plus two.'
- Subtracting numbers close together in value, through counting on to find the difference.



606 - 597 = ? *I* can count on from 597 to 606. The difference is 9.

# **Representing multiplicative relationships**

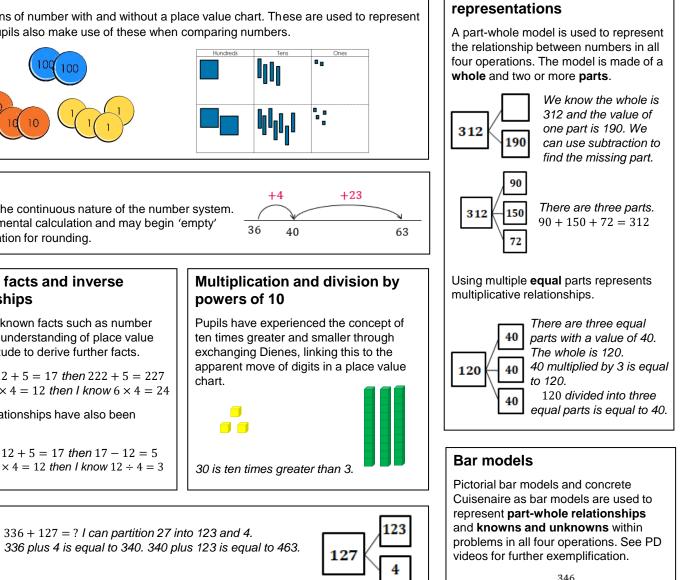
606

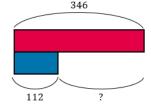
Pupils have represented multiplicative relationships concretely and pictorially, primarily through arrays, Cuisenaire and bar models. A focus on equal parts, the number of equal parts and the value of each part supports understanding of commutativity and inverse relationships. The representations and language structures support written strategies.

> There are four groups each with a value of 3. There are three groups each with a value of 4. I can see three, four times. I can see four, three times.

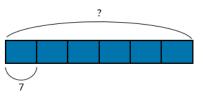
12 divided into groups of 4 gives three groups 12 shared into four groups gives 3 in each group

# Part-whole language and





I know the whole is 346, and one of the parts is 112. I do not know the value of the missing part. I can subtract 112 from 346.



The value of each part is seven and there are six equal parts. The whole is unknown. Six groups of seven is equal to 42. The whole is 42.

## **Representing fractions**

A range of concrete and pictorial representations have been used for fractions including fractions of a whole, as part of a set of objects and as part of a quantity such as a length or volume. Pupils can apply these representations to comparing, finding simple equivalence and adding and subtracting with the same denominator, as well as fractions of sets or quantities.

